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On the non-existence of totally localised intersections of D3/D5 branes in type IIB SUGRA

Leonardo Patiño and Douglas Smith

Department of Mathematical Sciences, University of Durham
Durham, DH1 3LE, U.K.
E-mail: e.l.patino-jaidar@durham.ac.uk, douglas.smith@durham.ac.uk

Abstract: In the present paper we study the most general configuration of intersecting D3/D5 branes in type IIB supergravity satisfying Poincaré invariance in the directions common to the branes and SO(3) symmetry in the totally perpendicular directions. The form of these configurations is greatly restricted by the Killing spinor equations and the equations of motion, which among other things, force the Ramond-Ramond scalar to be zero and do not permit the existence of totally localised intersections of this kind.

Keywords: Brane Dynamics in Gauge Theories, D-branes.

Contents

1. Introduction

The configurations of intersecting branes have proved to be of great importance in several applications in string theory and supergravity [1]. A very well known example of this is the Hanany-Witten construction [2] which describes a large class of supersymmetric gauge theories, where features such as the running of the gauge coupling are explained in terms of geometrical aspects of the brane configuration.

In the context of the Gauge/Gravity correspondence [3], configurations of fully localised intersecting branes have acquired increasing importance. Such configurations appear to have the elements to provide gravitational setups with dual gauge theories capable of reproducing some of the features of QCD.

Another example of the usefulness of totally localised solutions is the particular case of a AdS_4 brane embedded in an AdS_5 brane, which was used to construct a model of localised gravity in the brane [4].

The question of the existence of fully localised solutions for specific configurations is relevant, since even though there are a number of known solutions of this kind for specific types of branes [5−7], there are also arguments against the existence of them for other types [8, 9, 6].

It is therefore important to construct fully localised solutions of intersecting branes of different kinds, or to be able to prove such construction is not possible. The present paper is an effort in this direction.

Intersections of D3/D5 branes in type IIB supergravity have been studied in the past [10]. In that occasion to approach the problem, the Ramond-Ramond scalar was assumed to vanish as well as some of the components of the three and five-forms field strengths sourced by the branes. Partial results were found pointing towards the non-existence of fully localised branes intersections of this kind.

In the present work, other than Poincaré invariance on the directions common to the branes and SO(3) symmetry in the totally perpendicular directions, we don't make any initial assumptions about the solutions. So all the remaining restrictions, including the vanishing of the Ramond-Ramond scalar, come directly and exclusively from the Killing spinor equations and the equations of motion for the form fields involved in the configuration. As a consequence we find a slightly modified set of equations which imply the non-existence of totally localised intersections of this kind.

2. Brane probes

In the brane probe approximation the back reaction of the bulk to the presence of a brane is neglected [1]. Henceforth in this approximation, for a given supergravity solution, the introduction of a brane of the kind which is sourcing it shouldn't break further supersymmetry and in particular worldvolume supersymmetry should be preserved. For this to be the case the number of on-shell fermionic and bosonic degrees of freedom have to match and this requires the worldvolume action to be κ-symmetric. In the superembedding approach the imposition of this symmetry projects out half of the fields associated with the fermionic coordinates of the embedding of the world volume in the bulk.

In particular for a p-brane extending in the directions $01...p$ this projection condition reads [11, 12]

$$\widehat{\Gamma}_{01\cdots p}\epsilon_R = \epsilon_L \,, \tag{2.1}$$

where $\epsilon_{R,L}$ are chiral spinors standing for the supersymmetry variation parameters and in general in this paper, hatted objects will represent flat space elements.

The condition (2.1) has to hold for the supergravity solution sourced by the type and orientation of brane associated with it, and in the next section we'll see how to use this to find the supergravity solutions without the need of solving Einsteins equations.

3. The variation of the fermionic fields

An important property of branes and intersecting branes configurations is that they preserve a fraction of the supersymmetry. The precise fraction has to be found for each case and we will do this for ours in the next section, but we will describe the way it will be useful to us in the following paragraphs along the lines of [5].

In a bosonic background, the variation of the bosonic fields vanishes, therefore to explore the amount of supersymmetry preserved by the solution we have to consider only the variation of the fermionic fields. For type IIB supergravity we have to consider the

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variation of the dilatino λ and the gravitino ψ_M given [13, 14] respectively by

$$\delta\lambda = \frac{i}{\kappa}\Gamma^M P_M \epsilon^* - \frac{i}{24}\Gamma^{MNP} G_{MNP}\epsilon\,, \tag{3.1}$$

$$\delta\psi_M = \mathcal{D}_M\epsilon \equiv D_M\epsilon + U_M\epsilon + V_M\epsilon^*, \tag{3.2}$$

with

$$\begin{aligned} D_M &= \left(\partial_M + \frac{1}{4}\omega_M{}^{ab}\widehat{\Gamma}_{ab} - \frac{i}{2}Q_M\right), \\ U_M &= \frac{i\kappa}{48}\Gamma^{L_1\cdots L_4}F_{ML_1\cdots L_4}\,, \\ V_M &= \frac{\kappa}{96}\left(\Gamma_M{}^{L_1\cdots L_3}G_{L_1\cdots L_3} - 9\Gamma^{L_1L_2}G_{ML_1L_2}\right), \\ P_M &= f^2\partial_M B\,, \\ Q_M &= f^2\mathrm{Im}\left(B\partial_M B^*\right)\,, \\ f &= (1-BB^*)^{-1/2}\,, \end{aligned} \tag{3.3}$$

and B is related to the dilaton and the Ramond-Ramond scalar via the equation

$$C_0 + i\tau_2 = i\left(\frac{1-B}{1+B}\right). \tag{3.4}$$

Because of its convenience for the rest of the paper, the chiral spinors $\epsilon_{R,L}$ parameterising the variation have been written as a single complex spinor $\epsilon = \epsilon_R + i\epsilon_L$. The connection $\omega_M{}^{ab}$ is the spin connection, and it is contracted with a *flat space* gamma matrix because a and b are flat space indexes, even though, since these are totally contracted, it is not necessary to write any of the other objects in flat space terms.

For the solution to be supersymmetric (3.1) and (3.2) have to vanish. Therefore the amount of supersymmetry preserved by the solution can be obtained from the real dimensionality of the space spanned by the variation parameters compatible with the projection condition of the kind (2.1) for the specific configuration.

A tactic to find supersymmetric configurations is to obtain the corresponding projection conditions of the kind (2.1) and then impose them while solving the equations $\delta\lambda = 0$ and $\delta\psi_M = 0$, reducing therefore the number of solutions. It turns out often to be the case that this procedure determines the system completely, so even though the Einstein equations are not explicitly solved, they are automatically satisfied, as should be if these solutions are to exist at all.

The equations which are need to be solved in this scheme are much simpler than the Einstein equations, so this is how we will proceed in this paper.

4. Intersecting D5/D3 branes

Let's describe the system we are interested in by D5-branes extended in the directions $x^0, x^1, x^2, x^3, x^4, x^5$ and D3-branes along the directions x^0, x^1, x^2, x^6, so that they intersect over x^0, x^1, x^2 wile x^7, x^8, x^9 are totally perpendicular directions. All the branes are at the origin of the totally perpendicular directions, but the D5-branes can be spread over x^6, and the D3-branes over x^3, x^4, x^5.

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For this system there is a very convenient way to write the metric [10]

$$ds^2 = H_1^2\,\eta_{\mu\nu}dx^\mu dx^\nu + g_{\alpha\beta}dx^\alpha dx^\beta + D^2\left(dx^6 + A_\alpha dx^\alpha\right)^2 + H_2^2\delta_{ij}dx^i dx^j\,, \tag{4.1}$$

where Greek indexes from the middle of the alphabet like μ and ν run from 0 to 2, Greek indexes from the beginning of the alphabet run between 3 and 5, and lower case Latin characters take the values 7, 8 and 9. Upper case Latin indexes will run from 0 to 9.

Notice that on writing this metric we are assuming SO(3) symmetry on the totally perpendicular directions. If we take the metric to be independent of the common directions, then we will also have 2+1D Poincaré invariance. Nevertheless, the most general metric on the partially perpendicular directions can be expressed using the second and third terms in (4.1).

Now, the projection conditions for the D3 and D5 branes are respectively

$$\widehat{\Gamma}_{0126}\epsilon_R = \epsilon_L\,, \qquad \text{and} \qquad \widehat{\Gamma}_{012345}\epsilon_R = \epsilon_L\,. \tag{4.2}$$

Independently of the configuration, the spinors $\epsilon_{R,L}$ satisfy

$$\widehat{\Gamma}_{0123456789}\epsilon_R = \epsilon_R\,, \qquad \text{and} \qquad \widehat{\Gamma}_{0123456789}\epsilon_L = \epsilon_L\,, \tag{4.3}$$

since they are Mayorana-Weyl fermions.

Using some Dirac algebra it is easy to see that the conditions given by (4.2) and (4.3) can be succinctly written as

$$\widehat{\Gamma}_{0126}\epsilon = -i\epsilon\,, \qquad \widehat{\Gamma}_{3456}\epsilon = -\epsilon^*\,, \qquad \widehat{\Gamma}_{7896}\epsilon = -i\epsilon^*\,, \tag{4.4}$$

in terms of the complex spinor ϵ introduce earlier. This way of writing the projection conditions proved to be very convenient.

This is a good point to remember that we are not assuming anything about the five-form and three-form field strengths, so any restriction to their components will come from the corresponding equations of motion and the Killing spinor equations.

5. The Killing spinor equations

What follows is to write down explicitly the equations $\delta\lambda = 0$ and $\delta\psi_M = 0$, then by repeated use of (4.4) and Dirac manipulations get to extract the coefficients of the linearly independent combinations of $\widehat{\Gamma}$ matrices acting on ϵ and independently those acting on its complex conjugate ϵ^* [1].

A lengthly and not particularly enlightening calculation reveals the following. We can start with $\delta\psi_M = 0$ and pick the coefficients of the two indexes gamma matrices $\widehat{\Gamma}_{MN}$. It is worth noticing that these coefficients involve neither the dilaton nor the Ramond-Ramond scalar at all. From the resulting equations we see that the part of the metric given by $g_{\alpha\beta}$ has to be conformaly flat, and therefore we write it as diag(g^2, g^2, g^2), g being a general function.

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From the same coefficients we obtain the equations

$$
\begin{aligned}
2H_1^{-1}\partial_M H_1 + H_2^{-1}\partial_M H_2 + g^{-1}\partial_M g &= 0\,,\\
3H_1^{-1}\partial_M H_1 + 2H_2^{-1}\partial_M H_2 - D^{-1}\partial_M D &= 0\,,\\
4(g^{-1}\partial_\alpha g + D^{-1}\partial_\alpha D) - 4(g^{-1}\partial_6 g + D^{-1}\partial_6 D)A_\alpha - \partial_6 A_\alpha &= 0\,,\\
\partial_\alpha A_\beta - \partial_\beta A_\alpha - A_\alpha\partial_6 A_\beta + A_\beta\partial_6 A_\alpha &= 0\,,\\
\partial_i A_\alpha &= 0\,,
\end{aligned}
\tag{5.1}
$$

and the fact that the only non zero components of the five-form are $\widehat{F}_{0126\alpha}$, $\widehat{F}_{0126i}$ and those related to them by the self duality, $\widehat{F}_{345ij}$ and $\widehat{F}_{\alpha\beta789}$. All the other components of the five-form vanish identically.

The first and second equations in (5.1) can be solved respectively by setting

$$
g = H_1^{-2}H_2^{-1}\,, \qquad \text{and} \qquad D = H_1^3 H_2^2\,. \tag{5.2}
$$

Introducing $H \equiv g^4 D^4$ we can recast our remaining set of equations as

$$
\begin{aligned}
\partial_\alpha H - \partial_6(HA_\alpha) &= 0\,,\\
\partial_\alpha A_\beta - \partial_\beta A_\alpha - A_\alpha\partial_6 A_\beta + A_\beta\partial_6 A_\alpha &= 0\,,\\
\partial_i A_\alpha &= 0\,.
\end{aligned}
\tag{5.3}
$$

Using (5.2) we see that $H = H_1^4 H_2^4$, but it turns out to be useful to introduce $K \equiv H_1^{-2}H_2^2$, and keep H, K and A_α as the independent gravitational fields.

Still from the same components of the equations, we find for the five-form

$$
\begin{aligned}
\widehat{F}_{0126\alpha} &= \frac{\widehat{\varepsilon}_\alpha{}^{\beta\gamma}}{2}\widehat{F}_{789\beta\gamma} = \frac{H^{3/8}K^{3/4}\delta_\alpha^\delta}{4\kappa}\left(\partial_\delta K^{-1} - A_\delta\partial_6 K^{-1}\right),\\
\widehat{F}_{0126i} &= \frac{-\widehat{\varepsilon}_i{}^{jk}}{2}\widehat{F}_{345jk} = \frac{K^{1/4}\delta_i^l}{2\kappa H^{5/8}}\partial_l\left(H^{1/2}K^{-1/2}\right),
\end{aligned}
\tag{5.4}
$$

and for the three form

$$
\begin{aligned}
\widehat{G}_{6\alpha\beta} &= \widehat{\varepsilon}_{\alpha\beta}{}^\gamma\frac{\delta_\gamma^\delta}{\kappa H^{5/8}K^{1/4}}\left(\partial_\delta H - A_\delta\partial_6 H\right),\\
\widehat{G}_{345} &= \frac{-2K^{3/4}}{\kappa H^{9/8}}\partial_6\frac{H^{1/2}}{K^{1/2}}\,,\\
\widehat{G}_{6ij} &= \widehat{\varepsilon}_{ij}{}^k\frac{-iK^{1/4}\delta_k^l}{\kappa H^{9/8}}\partial_l H\,,\\
\widehat{G}_{789} &= \frac{i}{\kappa H^{5/8}K^{3/4}}\partial_6 K\,,
\end{aligned}
\tag{5.5}
$$

where we have used the elements of the zehnbein in terms of H, K and A_α to change from curved space-time components to flat space-time components, and the symbol $\widehat{\varepsilon}$ is the totally antisymmetric tensor in flat space, that is, we raise and lower indexes on it by using η_{MN}.

Finally from the components of the equation $\delta\lambda = 0$ with one index gamma matrices $\widehat{\Gamma}_M$ we find

$$\begin{aligned}
\widehat{P}_\alpha &= \frac{-\kappa}{8}\widehat{\varepsilon}_\alpha{}^{\beta\gamma}\widehat{G}_{6\beta\gamma}\,,\\
\widehat{P}_6 &= \frac{\kappa}{4}\left(\widehat{G}_{345} + i\widehat{G}_{789}\right),\\
\widehat{P}_i &= \frac{-i\kappa}{8}\widehat{\varepsilon}_i{}^{jk}\widehat{G}_{6jk}\,,
\end{aligned} \tag{5.6}$$

and the result that all the remaining components of $\widehat{\mathbf{G}}$ not listed in (5.5) vanish.

The rest of the equations coming from the linearly independent combinations of gamma matrices in the Killing spinor equations are redundant.

6. The vanishing of the Ramond-Ramond scalar

To completely determine the system we need to solve the equations of motion for the five-form and three-form field strengths. Let's start then by solving the equations given by

$$d\mathbf{F}_3 = 0\,, \tag{6.1}$$

where $\mathbf{F}_3$ is related to $\mathbf{G}$ by

$$\mathbf{G} = f\left(\mathbf{F}_3 - B\mathbf{F}_3^*\right). \tag{6.2}$$

To this end, using (3.3), (5.5) and (5.6) we see that

$$f^2\partial_M B = P_M = \frac{-1}{4H}\partial_M H\,. \tag{6.3}$$

Since f^2 and H are real, the imaginary part of B has to be just a constant. Writing $B = B_r + iB_0$ we find that the most general solution to (6.3) for constant B_0 is

$$B_r = \sqrt{1-B_0^2}\,\frac{1 - C_1 H^{\frac{1}{2}\sqrt{1-B_0^2}}}{1 + C_1 H^{\frac{1}{2}\sqrt{1-B_0^2}}}\,, \tag{6.4}$$

with

$$C_1 = e^{\frac{C}{\sqrt{1-B_0^2}}}\,. \tag{6.5}$$

Using this expression for B in (6.2) we can recover the real and imaginary parts of $\mathbf{F}_3$,

$$\begin{aligned}
\mathrm{Re}\,\mathbf{F}_3 = \frac{1}{2\sqrt{1-B_0^2}}\Bigg[&\left(\frac{1+\sqrt{1-B_0^2}}{\sqrt{C_1}H^{\frac{1}{4}\sqrt{1-B_0^2}}} + \left(1-\sqrt{1-B_0^2}\right)\sqrt{C_1}H^{\frac{1}{4}\sqrt{1-B_0^2}}\right)\mathrm{Re}\,\mathbf{G} +\\
&+\left(\frac{1}{\sqrt{C_1}H^{\frac{1}{4}\sqrt{1-B_0^2}}} + \sqrt{C_1}H^{\frac{1}{4}\sqrt{1-B_0^2}}\right)\times\\
&\times B_0\,\mathrm{Im}\,\mathbf{G}\Bigg] \qquad \text{and}\\
\mathrm{Im}\,\mathbf{F}_3 = \frac{1}{2\sqrt{1-B_0^2}}\Bigg[&\left(\frac{1}{\sqrt{C_1}H^{\frac{1}{4}\sqrt{1-B_0^2}}} + \sqrt{C_1}H^{\frac{1}{4}\sqrt{1-B_0^2}}\right)B_0\,\mathrm{Re}\,\mathbf{G} +\\
&+\left(\frac{1-\sqrt{1-B_0^2}}{\sqrt{C_1}H^{\frac{1}{4}\sqrt{1-B_0^2}}} + \left(1+\sqrt{1-B_0^2}\right)\sqrt{C_1}H^{\frac{1}{4}\sqrt{1-B_0^2}}\right)\mathrm{Im}\,\mathbf{G}\Bigg].
\end{aligned} \tag{6.6}$$

Equation (6.1) implies that the exterior derivative of these last two expressions has to vanish. Given the form of $\mathbf{G}$ it is not difficult to see that this vanishing can only be possible if the coefficients of the real part of $\mathbf{G}$ in (6.6) are identical or one of them vanishes, and the same thing applies to the coefficients of the imaginary part of $\mathbf{G}$. Examination of the coefficients leads to the fact that the only regular solution which satisfy these constrains is $B_0 = 0$, and since from (3.4) the Ramond-Ramond scalar is given by

$$C_0 = \frac{2B_0}{(1+B_r)^2 + B_0^2}\,, \tag{6.7}$$

we see that this implies the vanishing of the Ramond-Ramond scalar.

The expressions (6.6) then further simplify to

$$\mathrm{Re}\,\mathbf{F}_3 = H^{-1/4}\,\mathrm{Re}\,\mathbf{G} \qquad \text{and} \qquad \mathrm{Im}\,\mathbf{F}_3 = H^{1/4}\,\mathrm{Im}\,\mathbf{G} \tag{6.8}$$

We still have to solve the equations $d\,\mathrm{Re}\,\mathbf{F}_3 = d\,\mathrm{Im}\,\mathbf{F}_3 = 0$, but we already see that for these solutions to exist the Ramond-Ramond scalar *must* vanish.

Let's finish this section by noticing that B is not present in the expressions (6.8) but with these further simplifications we can solve for it straight away from (6.3) and use (3.4) to write down the solution for τ_2

$$\tau_2 = H^{1/2}. \tag{6.9}$$

7. The non-existence of totally localised solutions

Once we have seen that the Ramond-Ramond scalar vanishes, we can write down the equations of motion as

$$\begin{aligned} d\mathbf{F}_5 + \frac{\kappa}{4}(\mathrm{Im}\,\mathbf{F}_3 \wedge \mathrm{Re}\,\mathbf{F}_3) &= *\boldsymbol{\rho}_{D3}\,, \\ d\mathbf{F}_3 &= *\boldsymbol{\rho}_{D5}\,, \\ d*(\tau_2\,\mathrm{Re}\,\mathbf{F}_3) &= 4\kappa\mathbf{F}_5 \wedge \mathrm{Im}\,\mathbf{F}_3\,, \\ d*(\tau_2^{-1}\,\mathrm{Im}\,\mathbf{F}_3) &= -4\kappa\mathbf{F}_5 \wedge \mathrm{Re}\,\mathbf{F}_3\,, \end{aligned} \tag{7.1}$$

where $*$ is the Hodge star operator and $\boldsymbol{\rho}_{Dp}$ is the p+1-form given the density distribution of the Dp-branes.

To advance any further we notice that the conformal flatness we found for the part of the metric given by $g_{\alpha\beta}$ implies SO(3) symmetry in these directions, so if we introduce spherical coordinates on this three dimensional space, the only dependence on the coordinates will be through the radial coordinate r. We can do the same for the totally perpendicular directions, and denote the radial coordinate as ρ.

The result of rewriting the differential forms in terms of these coordinates is that after a straightforward calculation all of the equations given by the different componets of (7.1) reduce to a set of independent differential equations, being the source equations

$$\frac{1}{r^2}\partial_r\left[r^2(\partial_r K - A_r\partial_6 K)\right] + \frac{1}{\rho^2}\partial_\rho\left[\rho^2\partial_\rho(KH^{-1})\right] + \partial_6 K\left[H^{-1}\partial_6(H^{-1}K) + A_r\partial_6 A_r\right] = \rho_{D3}\,,$$

$$\text{and} \qquad \frac{1}{\rho^2}\partial_\rho\left(\rho^2\partial_\rho H\right) + \partial_6^2 K = \rho_{D5}\,, \tag{7.2}$$

along with the identities

$$(\partial_\rho H^1)\partial_6(H^{-1}K) = 0\,, \tag{7.3}$$

$$(\partial_\rho K^1)\partial_6(H^{-1}K) = 0\,, \tag{7.4}$$

$$(\partial_6 A_r)(\partial_6 K) = 0\,, \tag{7.5}$$

$$(A_r\partial_6 K - \partial_r K)(\partial_6 K) = 0\,, \tag{7.6}$$

$$\partial_\rho A_r = 0\,, \tag{7.7}$$

$$\partial_r H - \partial_6(A_r H) = 0\,, \tag{7.8}$$

$$\partial_6[H^{-1}\partial_6(H^{-1}K) + A_r\partial_6 A_r] - \frac{1}{r^2}\partial_r(r^2\partial_6 A_r) = 0\,, \tag{7.9}$$

where the ρ_{Dp} are functions coming from the pertinent components of the p+1-forms $\boldsymbol{\rho}_{Dp}$.

It is from these equations that the non-existence of totally localised solutions is apparent, but let's be explicit about it.

One way to see it is to start by considering K in the source equation of the D5-branes, and analyse the only two possible cases.

1) The first alternative is

$$\partial_6 K = 0\,, \tag{7.10}$$

so that the distribution is purely given by H. In this case $\partial_\rho H \neq 0$ if we want D5-branes at all, and $\partial_6 H \neq 0$ if these are to be localised on the x^6 direction. From (7.3) we see that these three conditions are not compatible.

2) The second case we need to analyse is

$$\partial_6 K \neq 0\,. \tag{7.11}$$

Localisation on ρ of the D5-brane requires

$$\partial_\rho K \neq 0\,, \tag{7.12}$$

which along with (7.4) implies

$$\partial_6(H^{-1}K) = 0. \tag{7.13}$$

On the other hand, (7.11), (7.5) and (7.6) imply

$$\partial_6 A_r = 0\,, \qquad \text{and} \qquad A_r\partial_6 K - \partial_r K = 0\,. \tag{7.14}$$

So we see that in the source equation for the D3-branes only the second term is different from zero. Localisation on r of the D3-branes would require $\partial_r(KH^{-1}) \neq 0$, but this is not the case, since equations (7.11), (7.14), (7.6) and (7.8) imply

$$\partial_r K = A_r\partial_6 K\,, \qquad \text{and} \qquad \partial_r H = A_r\partial_6 H\,, \qquad \text{so} \qquad \partial_r(KH^{-1}) = A_r\partial_6(KH^{-1}) = 0\,. \tag{7.15}$$

The last line is true because of (7.13).

We see then that, the first case is simply inconsistent, whereas in the second the localisation of the D5-branes implies the smearing of the D3-branes, which completes the proof on the non-existence of totally localised solutions for our case.

It is very easy to see, but worth commenting, that if we set to zero one or the other brane distribution densities, the remaining equations lead to the known (fully localised) solutions for only D5 or D3 branes configurations.

8. Why are there not localised solutions?

The reason why no totally localised solutions exist for certain configurations of intersecting branes has been discussed in the past in terms of the field theory associated with them in the near horizon limit. This discussion covers examples such as parallel D1- and D5-branes, for which a filed theoretical argument has been formulated which predicts that a D1-brane brought in from infinity will smear out as it approaches the D5-brane [9]. Using a weak field perturbative approach to a coupled Born-Infeld/bulk supergravity system, it has been formulated a perturbative expansion which applies to M2⊥M2 and M5⊥M5 intersections[6], and it was found that the perturbation theory does not converge for the the M2⊥M2 while it is well behaved for the M5⊥M5, indicating that fully localised solutions for the first case may not exist. Unfortunately the configuration we are treating here has not been considered in this discussion, though it has been commented [9] that there could be indications of a breakdown of holography when the dimension of the totally perpendicular space is three, which is precisely our case.

Notice that the configuration our computations are pointing to, is that of a totally localised D5-brane with a uniformly smeared D3-brane over its world volume spanning one extra dimension. Whether this smearing is related to a no-hair theorem for the D5-brane is far from clear to us yet, but this could be the case in analogy with the analysis of [15].

To properly understand which is the mechanism preventing these configurations from being totally localised, further investigation is necessary. A first step in this direction would be to separate the branes along one of the totally perpendicular directions, and then analyse the smearing as we bring the branes closer together.

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